A. Today's lectures reviews a few useful tools from micro-economics that provide a basis for sophisticated "undergraduate" analysis and for "simpe" graduate and post graduate analysis of a variety of public finance issues.
B. The lecture begins by introducing a somewhat novel net-benefit maximizing foundation model of rational choice that can be used to derive supply and demand curves and which provides a useful logical foundation for a variety of geometric, algebraic, and calculus representations of the burden of taxation.
C. After some developing the "basics" of micro economics, the tools are applied to analyze some "basic" properties of tax systems.

## I. The Fundamental Geometry of Net Benefit Maximizing Choice

A. Nearly all economic models can be developed from a fairly simple model of rational decision making that assume that individuals maximize their private net benefits.
i. Consumers maximize consumer surplus: the difference between what a thing is worth to them and what they have to pay for it. $\mathrm{CS}(\mathrm{Q})=\mathrm{TB}(\mathrm{Q})$ - TC(Q)
ii. Firms maximize their profit:, the difference in what they receive in revenue from selling a product and its cost of production: $\Pi=\operatorname{TR}(\mathrm{Q})$ TC(Q)
iii. This method of representing rational choice is useful for a variety of purposes in public policy analysis, although it produce models that are less able to represent purely market-based comparative statics.
B. The change in benefits, costs, etc. with respect to quantity consumed or produced is generally called Marginal benefit, or Marginal cost.
i. DEF: Marginal " X " is the change in Total "X" caused by a one unit change in quantity. It is the slope of the Total "X" curve. "X" $\in\{$ cost, benefit, profit, product, utility, revenue, etc.\}
ii. Important Geometric Property: Total "X" can be calculated from a Marginal "X" curve by finding the area under the Marginal 1 " X " curve over the range of interest (often from 0 to some quantity Q ). This property allows us to determine consumer surplus and/or profit from a diagram of marginal cost and marginal revenue curves.

C. Examples:
i. Given the marginal cost and marginal benefit curves in Figure 1, it is possible to calculate the total cost of $\mathrm{Q}^{\prime}$ and the total benefit of $\mathrm{Q}^{\prime}$. These can be represented geometrically as areas under the curves of interest. $\mathrm{TC}\left(\mathrm{Q}^{\prime}\right)=\mathrm{II}$; $\mathrm{TB}\left(\mathrm{Q}^{\prime}\right)=\mathrm{I}+\mathrm{II}$.
ii. Similarly, one can calculate the net benefits by finding total benefit and total cost for the quantity or activity level of interest, and subtracting them. Thus the net benefit of output $Q^{\prime}$ is $T B\left(Q^{\prime}\right)-T C\left(Q^{\prime}\right)=[I+I I]-$ [ II ] = I.
iii. Use Figure 1 to determine the areas that correspond to the total benefit, cost and net benefit at output $Q^{*}$ and $Q^{\prime \prime}$.
iv. Answers:
a. $\mathrm{TB}\left(\mathrm{Q}^{*}\right)=\mathrm{I}+\mathrm{II}+\mathrm{III}+\mathrm{IV}, \mathrm{TC}\left(\mathrm{Q}^{*}\right)=\mathrm{II}+\mathrm{IV}, \mathrm{NB}\left(\mathrm{Q}^{*}\right)=\mathrm{I}+\mathrm{III}$
b. $\mathrm{TB}\left(\mathrm{Q}^{\prime}\right)=\mathrm{I}+\mathrm{II}+\mathrm{III}+\mathrm{IV}+\mathrm{VI}, \mathrm{TC}\left(\mathrm{Q}^{\prime \prime}\right)=\mathrm{II}+\mathrm{IV}+\mathrm{V}+\mathrm{VI}$, $\mathrm{NB}\left(\mathrm{Q}^{\prime \prime}\right)=\mathrm{I}+\mathrm{III}-\mathrm{V}$
D. If one attempts to maximize net benefits, it turns out that generally he or she will want to consume or produce at the point where marginal cost equals marginal benefit (at least in cases where Q is very divisible).
i. There is a nice geometric proof of this. (The example above, C , nearly proves this. Note that $N B\left(Q^{*}\right)>N B\left(Q^{\prime}\right)$ and $N B\left(Q^{*}\right)>N B\left(Q^{\prime \prime}\right)$.)
ii. In the usual chase, a net-benefit maximizing decision maker chooses consumption levels $(\mathrm{Q})$ such that their own marginal costs equal their
own marginal benefits. They do this not because they care about "margins" but because this is how they maximizes net benefits in most common choice settings of interest to economists. (Another common choice that maximizes net benefits is $\mathrm{Q}^{*}=0$. Why?)
iii. This characterization of net benefit maximizing decisions is quite general, and can be used to model the behavior of both firms and consumers in a wide range of circumstances.
iv. Moreover, the same geometry can be used to characterize ideal policies if "all" relevant costs and benefits can be computed, and one wants to maximize Social Net Benefits.
E. That each person maximizes their own net benefits does not imply that every person will agree about what the ideal level or output of a particular good or service might be.
i. Most individuals will have different marginal benefit or marginal cost curves, and so will differ about ideal service levels.
ii. To the extent that these differences can be predicted, they can be used to model both private and political behavior:
a. (What types of persons will be most likely to lobby for subsidies for higher education?
b. What types of persons will prefer progressive taxation to regressive taxation?
C. What industries will prefer a carbon tax to a corporate income tax?)
F. One can use the consumer-surplus maximizing model to derive a consumer's demand curve for any good or service (given their marginal benefit curves) by: (i) choosing a price, (ii) finding the implied marginal cost curve for a consumer, (iii) use MC and MB to find the CS maximizing quantity of the good or service, (iv) plot the price and the CS maximizing $\mathrm{Q}^{*}$, and (v) repeat with other prices to trace out the individual's demand curve.
G. Similarly, one can use a profit maximizing model (another measure of net benefit) to derive a competitive firm's short run supply curve, given its marginal cost curve. Again, one (i) chooses a price (which is a price taking firm's MR curve), (ii) finds the profit maximizing output, (iii) plot P and $Q^{*}$, (iv) repeat to trace out a supply curve.

## II. Markets, Externalities, and Social Net Benefits

A. Market Demand can be determined by varying price and adding up the amounts that consumers want to buy at each price.
i. Market Demand curves for ordinary private goods, thus, can be shown to be "horizontal" sums of individual demand curves
ii. Similarly, Market Supply (for an industry with a fixed number of firms) can be derived by varying price and adding up the amounts that each firm in the industry is willing to sell at each price.
iii. Market Supply curves for ordinary private goods can be shown to be "horizontal" sums of individual firm supply curves.

- In the short and medium run, the number of firms in the industry can be taken as fixed.
- Long run supply varies according to whether one is in a Ricardian or Marshallian world (as developed further below).
B. Note that derived in this way, it is clear that:
i. Every market demand curve is (approximately) the sum of the marginal benefit curves of the individual consumers, because each consumer's demand curve is essentially his or her MB curve.
ii. Every short and middle run market supply curve is (approximately) the sum of the marginal cost curves of the individual firms in the market, because each firm's supply curve is essentially its MC curve.
iii. Consequently, market demand and supply curves can be used as social marginal benefit and marginal cost curves to estimate the net benefits realized by all firms and consumers in an industry.
C. In competitive markets, prices tend to move to "market clearing levels," that is to prices that set the total quantity supplied by all firms equal to the total amount demanded by consumers. (This defines equilibrium market $\mathrm{P}^{*}$, and $\mathrm{Q}^{*}$.)
i. In competitive markets, this occurs where the supply and demand curve cross.
ii. At any other price, there will either be surpluses (which tend to cause prices to fall) or shortages (which tend to cause prices to rise).
iii. Note that this is, in principle, an entirely decentralized process requiring governments to do nothing more than enforce property rights and contracts.
D. In the absence of externalities or market concentration, markets tend to produce social net benefit maximizing outputs!
i. Note that the "market clearing" price causes markets to produce the social net benefit maximizing level of output (in cases where there are not externalities, e.g. relevant costs or benefits).
- Q* sets social marginal benefit (the demand curve) equal to social marginal cost (the supply curve).
- This is one very widely used normative argument for using markets as a method of organizing the production of useful services.

ii. It bears noting that there are two different models of long run supply.
a. In Ricardian models of supply, the same geometry and logic can be used for long run supply.
- (Ricardian supply assumes that each potential supply has a given LR MC curve, that varies with the particular supplier, as farm fields and oil wells can be more or less costly to develop.)
- The same geometric logic can be used to develop LR supply in Ricardian markets. That is, the LR supply for Ricardian markets is approximately the industry's LR marginal cost curve.
b. In contrast LR supply in the Marshallian context occurs as identical firms (e.g. with identical MC and ATC curves) entry and exit the industry of interests.
- Incentives for exit and entry end when profits fall to zero.
- This implies that each firm is at the bottom of its LR ATC curves, which allows long run supply curves to be characterized as the industry's LR ATC rather than its LR MC.
- (This property also allows the equilibrium numbers of firms to be calculated for Marshallian industries using long run average cost curves of firms. In the long run, efficient sized firms are simply replicated until market demand is satisfied.)
iii. We will shift back and forth between the Ricardian and Marshallian long run perspectives according to the market at hand.
E. In cases where external costs exist, however, market outcomes will (often) fail to maximize social net benefits, because those costs will not be fully accounted for in the calculations of economic agents.
- In this case, either demand or supply will not include all marginal benefits or all marginal costs.
i. The existence of externality problems provides a normative basis for government policy (if one wants to maximize social net benefits).
- In cases where significant external costs exist at the margin (at Q*), markets will tend to over produce the output of interest relative to that which maximizes social net benefits.
- In cases where significant external benefits exist at the margin (at Q*), markets will under produce the service of interest relative to that which maximizes social net benefits.
- Governments might adopt policies to discourage production in the first case (perhaps with taxes) or encourage it (perhaps with subsidies) in the second case.


## III. A Review of Elementary Public Finance: The Burden of Taxation

A. Taxation is the primary method by which governments finance themselves.
i. Essentially all taxes transfer resources from the private to public sector, where government decision makers (both elected and unelected) will choose how those resources will be allocated between providing services and redistribution.
ii. Essentially all taxes shift resources to the government by threatening current resource holders (property owners, labor, international trading firms, etc.) with punishments of various sorts if they do not "give" their resources to the government's tax collectors.
a. In this sense, all taxes are coercive at the point of collection.
b. This contrasts with government bonds and ordinary fees for services, because such transactions are voluntary at the point of collection. Bond buyers and public service purchasers expect to be better off after the purchase, whereas tax payers normally feel worse off after paying the tax (although better off than had they not paid and been placed in jail).
c. On the other hand, insofar as taxes are used to fund desired public services, taxation as a method of government finance can be regarded as voluntary in much the same sense that the amounts paid stores for their products can be regarded as voluntary. In such cases, voters prefer to "tax themselves" to pay for desired governmental services, rather than go without those services.
iii. To the extent that government borrowing (sales of bonds) are repaid, even borrowing can be regarded as an implicit tax, because the government promises bond buyers that they will collect tax revenue in the future to pay interest and principal on the bonds.
iv. The usual non-tax sources of revenue involve sales of government services or assets to the public..

- For example, the U. S. central government (federal government) sells assets when it sells mineral, timber, and grazing rights to industry.
a. National parks are partially financed by charging admission.
B. The most important taxes for the federal government of the United States today are:
i. the income tax ( 1.168 trillion dollars in 2007)
ii. the payroll tax (used to finance social security) ( 873 billion dollars in 2007)
iii. corporate income taxes ( 342 billion dollars in 2007)
iv. excise taxes ( 57.1 billion dollars in 2007)
v. At the state and local levels of taxation in the United States, the most important taxes in 2007 were: the sales tax ( 414 billion), the property tax ( 370 billion), the income tax ( 275 billion).
vi. (Source: 2008 Statistical Abstract of the United States)

C. The burden of particular taxes can be measured in two ways:
i. First, it can be calculated as a cash payment--in much the same way that payments for ordinary goods are calculated.
a. (This is the most widely used measure by macro-economists, accountants, and newspaper reporters.)
b. (It is also occasionally implicitly used by public finance economists. When data on the slopes of relevant demand and supply curves are unavailable. In such cases, its often convenient as a first approximation to assume that supply is horizontal--as in a Marshallian competitive long run equilibrium--and so the full economic burden falls on consumers, as shown below.)
ii. Second, the burden of taxation can be calculated by determining the losses imposed on taxpayers as a consequence of the tax--that is to say the opportunity cost of the tax.
a. This is the approach used by most economists (most of the time).
b. From an economic perspective, the burden of an excise or income tax can be measured as the reduction of consumer surplus and profits induced by the tax.
- (This measure how much worse off consumers and firms are because of the tax itself, which ignores any benefits they may receive from the tax financed services.)
- (In an indifference curve representation of tax burden, burden is the change in utility associated with the tax.)
c. This measure of burden differs a bit from the money paid to the government in several ways.
- First, the total burden of a tax is normally larger than the amount of money that taxpayers send into the treasury.
- Most taxes have a deadweight loss, which can be measured as the extent to which "social surplus" is reduced by the existence of a particular tax, which as we will see depends partly on how the taxes are spent.
- Second, the distribution of the tax burden varies with market conditions (the slopes of the relevant supply and demand curves) rather than with who signs the check sent to the treasury.
iii. In this sense, tax payments are often made by persons or firms who do not write checks to the treasury, and who may not be "obviously" affected by a particular tax law..
a. For example, sales taxes are paid by firms in the sense that firms (or firm owners) actually write the checks deposited in the government's treasury. Thus, calculated as cash payments, one could say that the burden of a sales tax falls entirely on firms.
b. However, if firms simply increase their prices to pay for the tax, which is what they appear to do at the cash register, then the tax burden has really been "shifted" forward onto their customers, even though consumers never actually write checks for sales taxes and send them into the treasury.
c. In many cases, the persons most affected by a tax are not the persons who "directly" pay the taxes by writing out a check to the treasury or IRS!
D. Illustration of the economic burden of an excise tax:
i. Suppose that a market is initially in an equilibrium without taxes, so that demand equal supply at $\mathrm{P}^{*}$. In this case, there is no "tax wedge" between the price paid by consumers, Pc , is the same as that received by firms, Pf; so $\mathrm{Pf}=\mathrm{Pc}=\mathrm{P}^{*}$.
a. Now, suppose that an excise tax of $\mathbf{T}$ is imposed on each unit of the good sold in this market, as for example is done with tire sales in the US.
b. After the tax is imposed, $\mathrm{P} *$ is no longer the market clearing price:
c. If $\mathbf{T}$ is simply added to $\mathrm{P}^{*}$ by firms, consumers will purchase too little at their new price $\left(\mathrm{Pc}=\mathrm{P}^{*}+\mathrm{T}\right)$ to match supply, which would remain at Q*.
d. On the other hand, if firms simply "ate" the tax, they would provide too little of the good to meet demand (at their after tax price of $\mathrm{Pf}=\mathrm{P} *$ _ T). Supply would fall and demand would remain at $\mathrm{Q}^{*}$ if $\mathrm{Pc}=\mathrm{P}^{*}$ and $\mathrm{P}_{\mathrm{s}}=\mathrm{P}^{*}-\mathrm{T}$.
e. To clear the market, thus, firms have to receive less than $\mathrm{P}^{*}$ per item sold, and consumers have to pay more than $\mathrm{P}^{*}$.
f. At the new equilibrium output, the demand curve will be exactly $T$ dollars above the supply curve, and $\mathrm{Qd}(\mathrm{Pf}+\mathrm{T})=\mathrm{Qs}(\mathrm{Pf})$.
ii. This equilibrium output is shown in the diagram. At $Q^{\prime}$, supply equals demand, if the price paid by consumers is exactly $\mathbf{T}$ dollars higher than the amount firms receive $(\mathrm{Pf}=\mathrm{Pc}-\mathrm{T})$.
$-\mathrm{Q}^{\prime}$ units of the good are sold, with $\mathrm{Q}^{\prime}<\mathrm{Q}^{*}$.
a. At this equilibrium, there is a sense in which the tax has simply been passed onto consumers, because $\mathrm{Pc}=\mathrm{Pf}+\mathrm{T}$.
- However, there is another sense in which the burden of taxation is shared by firms and consumers, because both consumer surplus and profits have been diminished by the tax!
- Consumer Surplus falls from area I + II + VI (before the tax at $\mathrm{Q}^{*}$ ) to just area I after the tax is imposed and output falls to $Q^{\prime}$.
- Similarly, Profit falls from III + IV+ VII (before the tax at Q*) $^{*}$ ) to area IV (after the tax at $Q^{\prime}$ ).
b. The burden on consumers is II $+V I$, and that on firms is III $+V I I$.
c. Note that this distribution of the loss of consumer and firm net benefits occurs regardless of who actually writes the check to the state or federal treasury.
- Price movements ultimately determine the actual division of burden between firms and consumers.
- If firms send in the check, their effective "payment" is reduced by the increase in price paid by consumers.
- If consumers write out the checks, their effective "payment" is reduced by the price decrease absorbed by firms.
iii. The amount of revenue raised by the tax is $\mathbf{T}^{*} \mathrm{Q}^{\prime}$.
a. $Q^{\prime}$ units are sold and each pays a tax of $\mathbf{T}$ dollars.
b. The total tax revenue, $\mathbf{T Q}^{\prime}$, can be represented in the diagram area II + III in the diagram.
- (Note that II + III is the area of a rectangle T tall and Q' wide.)
iv. Notice that the tax revenue is smaller than the "surplus" lost by taxpayers (firms and consumers in the affected market).
a. The reduced profit plus the reduced consumer surplus equals $\{\mathrm{II}+\mathrm{VI}\}$ $+\{\mathrm{III}+\mathrm{VII}\}$.
b. The total burden of this tax is VI + VII larger than the tax revenue.
c. This area of "excess burden" is sometimes referred to as the deadweight loss of an excise tax.
E. Both the extent of the deadweight loss and the distribution of the tax burden vary with the slopes of the supply and demand curves.
i. Generally, more of the burden falls on the side of the market with the least price sensitive curves.
a. If the demand curve is less elastic than the supply curve, more of the burden falls on consumers than on firms.
- In the extreme case in which market demand is completely inelastic or the industry supply curve is completely elastic, all of the burden falls on consumers!
b. On the other hand if the demand curve is very elastic, because good substitutes exist, or the supply curve is relatively inelastic then more of the burden tends to fall on the firm.
- In the extreme case in which the market supply of the product of interest is completely inelastic or consumer demand is perfectly elastic, all of the burden falls on suppliers.
ii. The excess burden of a tax tends to increase with the price sensitivity (slope or elasticity) of the demand and supply curves.
F. Both supply and demand tend to be more elastic in the long run than in the short run, consequently, the excess burden of taxation tends to be larger in the long run than in the short run.
i. In cases in which long run and short run demand are the same, the fact that long run supply is relatively more price sensitive (elastic) than short run supply implies that the burden of a new tax or increase in tax tends to be gradually shifted from firms to consumer in the long run.
- Many competitive markets have perfectly elastic supply curves in the long run, which implies that narrow taxes on such products are shifted entirely to consumers in the long run.
ii. There are, however, also cases in which consumer demand is more price elastic in the long run than in the short run (as when demand for a good is determined in part by consumer capital goods, like automobiles).
- In such cases, a tax such as a gasoline tax may be gradually shifted from consumers to firms (owners of capital and natural resources) in the long run.
iii. In cases where both sides of the market (firms and consumers) are more price elastic in the long run than in the short run, the shift of burden will reflect their relative ability to adjust.
iv. However, all such long run adjustments imply that deadweight losses to narrow taxes, such as an excise tax, are larger in the long run than in the short run.
v. Illustrations: effects of an excise tax in the short run and long run for different kinds of markets


a. Note that in the first case, supply is more elastic in the long run than in the short run, so the initial effect of the tax is largely on firms, but in the long run the burden is shifted to consumers.
- The after tax price falls at first for firms, but rises back to P*.
- The price to consumers rises just a bit at first, but rises to $\mathrm{P}^{*}+\mathrm{Pc}$ in the long run.
b. The second case is the case where demand is more price sensitive (elastic) in the long run than in the short run, but because supply is completely elastic in both the long and short run, the burden falls entirely on consumers in both the short and long run.
c. As an exercise, construct a case in which the burden falls entirely on firms in both the long and short run.
vi. In some cases, losses of consumer surplus may occur in other markets as a result of excise taxes.
- For example high gasoline taxes encourage bicycle purchases, which tend to increase the price paid for bicycles, at least in the short run.
- However, profits rise by nearly as much as the consumer surplus falls, so we will ignore these secondary effects in most of our analysis of tax burdens in this class.


## IV. A Review of Elementary Normative Principles of Taxation

A. The ideas summarized in these diagrams are have often been used to characterize "normative theories" of taxation.
B. For example, one normative theory of taxation was proposed by Frank Ramsay in 1927. He argued that a system of excise taxes should attempt to minimize the excess burden of the tax system.
i. A Ramsay tax system imposes higher taxes on markets with relatively inelastic supply and demand curves, and relatively lower taxes on markets with relatively large price sensitivities.
ii. If markets with perfectly inelastic demand or supply curves exist, government services can be financed without any deadweight loss at all, if taxes on such goods can generate sufficient revenues.
a. (Remember that taxes on products with inelastic supply or demand curves generate no deadweight losses.)
b. A special case of such a tax is a tax on land--which is sometimes called a Georgist tax after Henry George who proposed financing government entirely with land taxes. The supply of land, after all, is perfectly inelastic (ignoring dikes and dumps).
c. (Analyze the limitations, if any, of a Georgist land tax. Where does the value of a piece of land come from? Would there be allocative affects across different types of land? Would a Georgist land tax be neutral even if it is a Ramsay tax?)
d. (Given the possibility of international emigration, can their actually be a tax that has no dead weight loss? Discuss.)
C. It has also been argued that a tax system should not directly affect relative prices across markets (see the indifference curve analysis in the appendix).

## i. That is to say, a tax system should be NEUTRAL

a. A perfectly neutral tax system would not affect private sector decisions across markets for private goods and services, because it would not affect relative prices faced by firms or consumers (although it does, of course, produces revenues for the government).
b. In this case, a government that tried to finance itself via a system of excise taxes would impose excise taxes so that prices increased by the same proportion in every market taxed.
c. Alternatively, the government could look for somewhat narrower tax sources that do not have relative price effects, such as a lump sum or head tax.
d. (The geometry of lump sum taxes and other nearly neutral taxes can be illustrated a bit more easily using indifference curves and budget constraints, as is done in the Appendix below.)

- (Nonetheless, systems of excise taxes that generate a proportionate increase in all prices faced by consumers can clearly be illustrated with the tools developed above using demand and supply curves for several markets.)
D. Another normative theory of taxation argues that one cannot determine the proper division of the tax burden without thinking about the services that will be provided.
i. For example, Lindalh argues in favor of a benefit tax, that is a tax that imposes the greatest burden on those who receive the most valued services should pay the highest taxes.
ii. Under an ideal Lindalh tax system, each person's marginal tax rate would be set equal to the marginal benefits she or he receives from government services.
iii. James Buchanan (who won a Nobel Prize in economics while a professor at GMU, partly for his contributions to public finance) tends to agree with Lindalh.
a. Buchanan argues that proper accounts of tax burden--should focus on net tax burden--that is, they should take account of the services financed by taxes as well as the taxes paid.
b. For example, if a person receives an especially valuable service from the government, it is possible that his or her "true" net tax burden is negative. Others who receive no services of value, might have positive net tax burdens.
c. Ideally, all citizens would bear "negative" tax burdens in the sense that each person should receive services that are considered to be more valuable than the taxes paid.
d. (We will take up the demand and supply of government services later in the course.)
E. Other normative principles of taxation come are rooted in social norms or political philosophies of various kinds--often dealing with fairness (or equity).
i. For example, many argue that persons should pay based on their "ability to pay."
a. This notion of fairness tends to imply progressive income taxes.
b. For example, a "fair tax" might be one that caused all taxpayers should all sacrifice approximately the same "utility" (rather than net benefits) when they pay their taxes.
- (Since the marginal utility of money tends to be smaller for rich persons than poor persons, more money would be collected from rich persons than from poor persons.)
- (That is, taxes should be progressive rather than regressive)
ii. Others suggest that fairness requires all persons to pay be treated the same way under a tax system.
- (This notion of fairness tends to imply a flat tax--a proportional tax on income.)


## A. Definitions:

a. A progressive tax is a tax whose average burden increases as the taxable base owned by an individual increases. [Such taxes often have marginal tax rates that increase with the base (increase with income), although not all progressive taxes have this property. Most income tax systems in industrialized countries are somewhat progressive.]
b. A proportional tax is a tax whose average tax burden does not change with income. (Such taxes normally have a constant marginal tax rate, as true of most sales taxes and some income taxes. A flat (proportional) tax on income has the form: $\mathrm{T}=\mathrm{tY}$.)
c. A regressive tax is a tax whose average tax burden falls with income. Such taxes often have declining marginal tax rates with ownership of the taxable base, however, not all regressive taxes have this property. An example of a regressive tax in the US is the social security tax--which has a cap on taxable income.

## B. Definitions and Relationships:

- The tax base, B, is that which is taxed. (taxable income, sales of final goods and services, profits, property, gasoline, etc.)
- The average tax rate of a particular tax often varies with an individual's holding of the taxable base. If an individual pays tax Ti on a holding of Bi , his average tax rate is $\mathrm{Bi} / \mathrm{Ti}$. (If $\mathrm{Ti}=\$ 50$ and $\mathrm{Bi}=$ 200 , the average tax rate for this tax is $50 / 200=0.25$ or $25 \%$.)
- The marginal tax rate of a particular tax is the change in taxes owed for a one unit increase in holdings of the taxable base, $\Delta T / \Delta B$. (So, if a tax payer earning 50,000/year pays a tax of 10,000 and a taxpayer earning 50001 pays a tax of $10,000.50$, his or marginal tax rate is $0.50 / 1=50 \%$. Fifty percent of each additional dollar earned is taken


## from the "last" dollar of income earned by a taxpayer earning

 50,000/year.)a. Diagramming average and marginal tax schedules:

- If MTR is above ATR, then that ATR curve will be rising (the marginal tax rate will be pulling the average up).
- If MTR is below ATR, then the ATR curve will be falling (the marginal tax rate will be pulling the average down).
- -If the MTR = ATR, the ATR will be neither rising nor falling.
b. Since individual decisions are determined by marginal cost and marginal benefits at various quantities, it is the marginal tax rate rather than the average tax that directly affects tax payer behavior in most cases.
- (Thus, one argument in favor of proportional, or indeed, regressive taxes, is that they may have smaller effects on economic activities than a revenue equivalent progressive tax.)
A. (Peckman's estimates of the effective average and marginal tax rates faced by a typical American tax payer, often look a bit like this odd tax schedule.)
i. (As an exercise try to determine what the marginal tax schedule that corresponds to this average tax schedule looks like.)
ii. (Explain briefly why Peckman finds regressive ranges of taxation at both the highest and lowest ranges of income.)
B. Other normative tax theories are unconcerned with the fairness of the tax system and argue that a tax system should attempt to promote economic growth--or at least minimize the reduction in growth associated with raising a given amount of revenue.
i. Such persons often favor consumption taxes in order to encourage saving and investment.
ii. (The effects of a consumption tax on investment is easiest to illustrate with indifference curves and budget constraints, but the intuition behind the effect is simply based on supply and demand. If the price of saving falls relative to consumption, individuals will consume less and save more. And if savings increase, capital will be more rapidly accumulated, which leads to higher income levels and growth rates.)


B (taxable base)
V. APPENDIX: Analysis of Tax Effects Using Indifference Curves
A. The behavior affects of an excise tax can also be analyzed with indifference curves and budget constraints.
B. Suppose that there are two goods, Q and X , both of which the consumer normally uses.
i. Our previous analysis implies that the effect of an excise tax on a typical consumer is to raise the price of the taxed good from $\mathrm{P}^{*}$ to Pc.
ii. This increase in price affects the location of each consumer's budget set.
iii. It rotates the budget constraint from the untaxed end of the budget constraint and generates a new budget constraint that lies inside the original one at all points where the consumer purchases positive quantities of the taxed good.
iv. Illustration.
v. Suppose that "A" is the original bundle consumed by this consumer.
a. In this drawing the tax has increased price of good 1 from P1 to P1' (this price effect is taken from a supply and demand diagram)

- In the case drawn, the new higher price causes the consumer to purchase bundle $\mathbf{B}$ instead of A. (Indeed, A is no longer feasible.)
b. If instead of an excise tax on good 1 a lump sum tax (or wealth or sales $\operatorname{tax}$ ) had been used, the budget constraint would have shifted toward the
axis, but the new budget constraint would have the same slope as the original one.
- The "revenue equivalent" lump sum tax passes through point $\mathbf{B}$ and is parallel to the original (pre tax) budget constraint.
- Note that a lump sum tax, would have allowed the individual to purchase a bundle like $\mathbf{C}$ which is on a higher indifference curve (not drawn) than bundle B.
- This loss in utility (from being on a lower indifference curve) is another measure of the excess burden of a non-neutral tax on consumers.
c. Much of the deadweight loss is a consequence of reduction in purchases of the taxed good, particularly that part which was generated by the "relative price" effect of the excise tax.
- You learned in micro economics that every price increase has both a (relative price) substitution effect and a wealth effect on purchases of the good whose price has increased.
- An excise tax that affects consumer prices has both a (relative price) substitution effect and an income effect on purchases of the good whose price has increased because of a tax.
- A lump sum tax only has an income effect.
C. The behavioral effect of a general tax and a lump sum tax tends to be smaller than that of an excise tax, because these taxes have only a wealth effect.
i. A revenue neutral lump sum tax, a (neutral) general sales tax, and an income tax all shift each consumer's budget constraint towards the origin, but these taxes do not affect the slope of the consumer's budget constraint.
ii. Consequently, general taxes and lump sum taxes tend to have a smaller effect on behavior than excise taxes that raise the same amount of revenue. (There is no "substitution effect.")
D. Some Useful Algebra.
i. The slope of the budget lines can be calculated for the lump sum, sales and income taxes.
a. Recall that slope is "rise over run."
b. In the case without taxes, the slope of the budget line is -(W/P1) / (W/P2), which simplifies to - P2/P1.

c. In the case of a lump sum tax, the endpoints of the new budget line are (W-T)/P2 and (W-T)/P1.
- The slope of the new budget constraint is -[(W-T)/P1]/[ (W-T)/P2] which equals - P2/P1. (Show this algebraically.)
d. In the case of a an income tax, where W is treated as income, the after tax income is $(1-\mathrm{t}) \mathrm{W}$, so the endpoints of the new budget line are $((1-t) \mathrm{W}) / \mathrm{P} 2$ and $((1-\mathrm{t}) \mathrm{W}) / \mathrm{P} 1$.
- The slope of the new budget line is: $-[(1-\mathrm{t}) \mathrm{W}) / \mathrm{P} 1] /[((1-\mathrm{t}) \mathrm{W}) / \mathrm{P} 2]=-\mathrm{P} 2 / \mathrm{P} 1$.
e. In the case of a general sales tax the new after tax prices will be approximately $(1+\mathrm{t}) \mathrm{P} 1$ and $(1+\mathrm{t}) \mathrm{P} 2$. (What assumptions about supply and demand are sufficient for this to be exactly true?)
- The slope of the new budget line will be $-[(\mathrm{W}) /(1+\mathrm{t}) \mathrm{P} 1] /[((1-\mathrm{t}) \mathrm{W}) /(1+\mathrm{t}) \mathrm{P} 2]$, which again can be shown to equal -P2/P1.


## EC 950: Handout 2: A Review of a Few Useful Geometric Tools from Microeconomics

f. All three of these taxes are "neutral" with respect to the choice illustrated in our diagram.

- None of these taxes change the relative prices of goods 1 and 2. It remains -P2/P1 in each case.
- Note however that sales taxes have an effect on a consumers decision to save, and income taxes have an effect on a consumer's decision to work.)
E. In some cases, however, the purposes of a tax may be to change behavior.
i. In such cases, excise taxes and other "marginal" taxes will be more effective at altering behavior than lump sum or general taxes.

